

Cambridge International AS Level

MATHEMATICS**9709/22**

Paper 2 Pure Mathematics 2

October/November 2024**MARK SCHEME**Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of **12** printed pages.

PUBLISHED**Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

PUBLISHED**Mathematics Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

PUBLISHED**Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
 - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
 - The total number of marks available for each question is shown at the bottom of the Marks column.
 - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
 - Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	Apply logarithms correctly and apply power law at least once	*M1	
	Obtain $y = \frac{7 \ln 6}{8 \ln 5} x$ or equivalent perhaps involving decimals	DM1	May be implied by 0.97, 0.973 seen. May use a different base.
	Obtain $k = 0.974$ or state $y = 0.974x$	A1	Or greater accuracy.
		3	

Question	Answer	Marks	Guidance
2(a)	Differentiate to obtain form $k \sin 3x \cos 3x$ or $k \sin 6x$	M1	
	Obtain correct $24 \sin 3x \cos 3x$ or $12 \sin 6x$	A1	
	Substitute $x = \frac{1}{4}\pi$ to obtain -12	A1	
		3	
2(b)	Express integrand in form $k_1 + k_2 \cos 6x$	M1	Where $k_1 k_2 \neq 0$.
	Obtain $2 - 2 \cos 6x$	A1	
	Integrate to obtain $2x - \frac{1}{3} \sin 6x$	A1	OE
		3	

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Question	Answer	Marks	Guidance
3	Use product rule to differentiate $6e^{-x}y^2$	M1	Allow correct use of quotient rule. Must have $\frac{dy}{dx}$ from implicit differentiation.
	Obtain $-6e^{-x}y^2 + 12e^{-x}y \frac{dy}{dx}$	A1	SOI
	Obtain $+2e^{2x} - 12 \frac{dy}{dx}$	B1	May see separately. $+2e^{2x} - 12 \frac{dy}{dx} + 7$ scores B0.
	Rearrange correctly to obtain $\frac{dy}{dx} = \dots$	M1	(Correct equation: $-6e^{-x}y^2 + 12e^{-x}y \frac{dy}{dx} + 2e^{2x} - 12 \frac{dy}{dx} = 0$) Must be at least one $\frac{dy}{dx}$ from implicit differentiation present. May already have used substitution $\frac{dy}{dx} = \frac{6y^2e^{-x} - 2e^{2x}}{12e^{-x}y - 12}$. M0 for inclusion of an incorrect $\frac{dy}{dx}$.
	Substitute for x and y to obtain an exact final answer	M1	Must be at least one $\frac{dy}{dx}$ from implicit differentiation present.
	Obtain $\frac{5}{2}$ or 2.5	A1	
		6	

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Question	Answer	Marks	Guidance
4(a)	Show increasing curve above x -axis for $y = 1 + e^{2x}$	*B1	And appearing in first and second quadrants.
	Show V-shaped graph with vertex on positive x -axis and only one point of intersection with first curve	DB1	With modulus graph crossing y -axis above first graph.
		2	
4(b)	State or clearly imply $1 + e^{2x} = 4 - x$	B1	
	Arrange to confirm $x = \frac{1}{2} \ln(3 - x)$	B1	AG – necessary detail needed. Do not condone incorrect use of logs.
		2	
4(c)	Use iterative process correctly at least once	M1	
	Obtain final answer 0.465	A1	Answer required to exactly 3 sf.
	Show sufficient iterations to justify answer or show a sign change in the interval $[0.4645, 0.4655]$	A1	
		3	

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Question	Answer	Marks	Guidance
5(a)	Substitute $x = -2$ and equate to zero	M1	$-8a + 4b + 2a + 8 = 0$
	Substitute $x = 2$ and equate to 24	M1	$8a + 4b - 2a + 8 = 24$
	Obtain $-6a + 4b + 8 = 0$ and $6a + 4b - 16 = 0$	A1	OE
	Obtain $a = 2$ and $b = 1$	A1	
		4	
5(b)	Divide by $x + 2$ at least as far as the x term	M1	OE
	Obtain $(x + 2)(2x^2 - 3x + 4)$	A1	SOI
	Conclude with reference to root -2 , discriminant is -23 and no further root	A1	Or complete equivalent.
		3	
5(c)	State $\operatorname{cosec} \theta = -4$	B1	May be implied by $\sin \theta = -\frac{1}{4}$
	Attempt to find at least one value of θ from $\sin \theta = \pm \frac{1}{4}$	M1	Allow for 14.5, 14.4.
	Obtain -14.5 only and no others in the range	A1	Or greater accuracy (14.4775...).
		3	

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Question	Answer	Marks	Guidance
6(a)	Use y-values $\sqrt[3]{7}$, $\sqrt[3]{12}$ and $\sqrt[3]{27}$, or decimal equivalents	B1	1.913, 2.289, 3
	Use correct formula, or equivalent, with $h=1$	M1	May see 2 separate trapezia (2.1....+ 2.65...).
	Obtain 4.75	A1	
		3	
6(b)	Integrate to obtain form $k \ln(2x+5)$	M1	
	Obtain correct $\frac{27}{2} \ln(2x+5)$	A1	Condone inclusion of working for area in part (a) .
	Apply limits 0 and 2 to obtain $\frac{27}{2} \ln \frac{9}{5}$ or exact equivalent of required form and no extra terms	A1	
		3	
6(c)	Obtain 3.19	B1 FT	Following answers to (b) and (a) . If incorrect answers for (a) and/or (b) , then need to see <i>their (b)</i> (with no extra terms) – <i>their (a)</i> .
		1	
6(d)	State under-estimate ...	*B1	
	... because (a) is over-estimate due to tops of trapezia being above curve	DB1	Or similarly detailed comment.
		2	

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Question	Answer	Marks	Guidance
7(a)	Expand to obtain $2\sin^2 \theta + 2\sqrt{3} \sin \theta \cos \theta$	B1	Needs to be simplified but may be implied by later work.
	Attempt to express in terms of $\sin 2\theta$ and $\cos 2\theta$	*M1	Needs to be in the form $k + p \cos 2\theta + q \sin 2\theta$.
	Obtain $1 - \cos 2\theta + \sqrt{3} \sin 2\theta$	A1	
	Obtain $R = 2$	A1 FT	Following <i>their</i> $p \sin 2\theta + q \cos 2\theta$ form.
	Use appropriate trigonometry to find α	DM1	For <i>their</i> $p \sin 2\theta + q \cos 2\theta$ form. Allow for 60° .
	Obtain $1 + 2 \sin(2\theta - 30)$	A1	
	Alternative Method for Question 7(a):		
	Expand to obtain $2\sin^2 \theta + 2\sqrt{3} \sin \theta \cos \theta$	B1	Needs to be simplified.
	For expansion of $a + R \sin(2\theta - \alpha)$ and comparison with $2\sin^2 \theta + 2\sqrt{3} \sin \theta \cos \theta$	*M1	Need comparison of at least 2 like terms: $R \sin \alpha = 1$, $R \cos \alpha = \sqrt{3}$, $a - R \sin \alpha = 0$.
	$R \sin \alpha = 1$ and $R \cos \alpha = \sqrt{3}$ leading to values of R and α	DM1	
	Obtain $R = 2$	A1 FT	
	Obtain $\alpha = 30^\circ$ and $a = 1$	A1	
	Obtain $1 + 2 \sin(2\theta - 30)$	A1	
		6	

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Question	Answer	Marks	Guidance
7(b)	State $\sin(2\theta - 30) = -\frac{6}{10}$	*B1 FT	Following <i>their</i> answer to part (a). Must be using $\sin(2\theta - \alpha) = -\frac{1}{5}$ – <i>their</i> (a). Must have a value for a .
	Attempt complete method to find smallest positive value	DM1	
	Obtain 123.4 only	A1	Or greater accuracy.
		3	